Abstract—Exploiting physical layer characteristics to enhance or complement authentication strength in wireless networks has been attracting research attention recently. Existing physical layer authentication mechanisms mainly tackle single-hop communications. In this paper, we propose two physical layer challenge-response authentication mechanisms for wireless networks with relay. One mechanism, named PHY-CRAMR, is an extension of the existing PHY-CRAM protocol. It fully utilizes the randomness, reciprocity, and location decorrelation features of the wireless fading channel to hide/encrypt the challenge response messages at the physical layer, and is immune to outside attacks with a trusted relay. The other novel mechanism, named PHY-AUR, exploits randomness, coherence, and location decorrelation properties of wireless fading channel to securely convey the product of the channel state information on consecutive links and uses the fading channel to encrypt challenge and response messages. PHY-AUR is immune to both outside and inside attacks with an untrusted relay. Both PHY-CRAMR and PHY-AUR adopt OFDM technique to modulate the authentication key and challenge-response messages on subcarriers. Physical layer pilots and preambles are eliminated to prevent an attacker from gaining knowledge about the channel state information, and as a result prevent the authentication key from being revealed to untrusted attackers. We analyze the security strength of both mechanisms and conduct extensive simulations to evaluate them. It shows that both PHY-CRAMR and PHY-AUR can achieve both a high successful authentication rate and low false acceptance rate, and the performance improves as the signal to noise ratio (SNR) increases.

Index Terms—Physical-layer security, challenge-response authentication, relay network, wireless fading channel, OFDM

I. INTRODUCTION

With the rapid advancement of wireless communication technology and ever-increasing mobile and pervasive applications, it becomes increasingly important and challenging to secure wireless communications. Authentication is usually the first step to establish a secure communication between two parties. Recently, there has been an increasing interest in complementing or enhancing authentication in wireless networks by exploiting unique physical layer characteristics [1]–[11]. Physical layer authentication/identification benefits a number of wireless applications such as wireless forensics [12], identity-based attack detection [13], and location decorrelation features of the wireless fading channel to mask the authentication key, and exploit channel reciprocity to cancel out the channel effect using inverse operations such that the verifier can decode the secret without knowing the channel state information.

In this paper, we propose two physical layer challenge-response authentication mechanisms for two-hop wireless networks involving a relay. We first propose a mechanism, named PHY-CRAMR (PHYysical layer Challenge Response Authentication Mechanism with Relay), which is an extension of the existing PHY-CRAM protocol [11]. It fully utilizes the randomness, reciprocity, and location decorrelation features of the wireless fading channel to hide/encrypt the challenge response messages at the physical layer, and is immune to outside attacks assuming the relay is trustworthy. The basic idea of PHY-CRAMR is to use a random number and channel fading to mask the authentication key, and exploit channel reciprocity to cancel out the channel effect using inverse operations such that the verifier can decode the secret without knowing the channel state information.

In order to tackle an untrusted relay node, who attempts to break the authentication key or impersonate legitimate users, we further propose a novel authentication mechanism, named PHY-AUR (PHYysical layer Authentication with Untrusted Relay). It exploits randomness, coherence, and location decorrelation properties of the wireless fading channel to securely convey the product of the channel state information on the two relay links and use the fading channel to encrypt challenge and response messages. PHY-AUR is secure against both outside and inside attacks with an untrusted relay.

PHY-CRAMR and PHY-AUR share a unique feature that, it eliminates channel coding, channel estimation and frequency offset compensation in the challenge-response messages. This feature not only simplifies the baseband design, but also prevents the outside and inside attackers from knowing the channel state information, thus provides strong security strength.

We summarize our major contributions as follows:

- We propose two physical layer challenge-response authentication mechanisms, PHY-CRAMR and PHY-AUR, for two-hop wireless networks with a relay in section IV and V.
- We conduct extensive simulation to evaluate the performance of proposed two mechanisms under different channel conditions, key lengths, and signal to noise ratios (SNRs), as reported in section VI.
- The security strength of PHY-CRAMR and PHY-AUR are analyzed and evaluated under various attacks in section IV-E and V-C.

II. RELATED WORK

A. Physical Layer Authentication/Identification

Existing physical layer authentication/identification schemes mainly focus on single-hop wireless communications, and can be generally categorized into four types: (1) the ones based on transceiver hardware differences, i.e., RF fingerprinting [6]–[8],...
The document discusses various authentication mechanisms for two-hop wireless networks, focusing on both physical layer and conventional challenge-response methods. It mentions PHY-CRAMR and PHY-AUR as proposed protocols that utilize physical layer properties to hide the shared secret used for authentication, which is fundamentally different from the conventional ones. These mechanisms are designed to be secure even when the relay is untrusted.

1) RF Fingerprinting for Device Identification: Most wireless devices have unique and uncloneable impairments that could be used for device identification. These impairments, with the name RF fingerprinting, may be caused by either transient behaviours of amplifiers or imperfection of constellation [7].

Unfortunately, RF fingerprinting is unsafe under impersonation attack [8]. To attack the existing RF fingerprinting schemes, an attacker does not necessarily reproduce a legitimate radio, but only needs to reproduce/replay the signal used for RF fingerprint verification. Furthermore, measurements on RF fingerprinting is expensive, since it needs a high-end signal analyzer to extract the subtle differences in the signals. Lastly, it usually requires a relatively stationary channel condition in order to accurately extract the RF fingerprint. That is, its performance tends to deteriorate in a dynamic environment.

2) Wireless Channel Based Authentication: Channel state information (CSI) between different transmitter-receiver (Tx-Rx) pairs are different, and may be used for authentication [2], [3]. This type of authentication requires that locations and CSI of legitimate users are known, channel sounding are fast enough compared with channel coherence time $T_C$, or the number of channel sounding samples is large enough to overcome the time-varying effect. Moreover, false acceptance rate of such method is high when mimicry attackers are very close to legitimate users [17].

In our protocols, PHY-CRAMR does not require channel sounding, while PHY-AUR conducts channel sounding on-the-fly. Both protocols neither require legitimate users to be at specific locations nor need to measure CSI of legitimate users first. Our protocols exchange only two messages during authentication, and can be finished well within time interval $T_C$ to ensure channel reciprocity.

In time-varying channels, CSI or received signal strength (RSS) may be used for message authentication [1], [4], while the proposed protocols in this paper study user authentication.

3) Physical Layer Signal Watermarking: Physical layer signal watermarking or fingerprinting embeds a cryptography based authentication code or tag into the original data signal [9], [10]. By doing this, conventional wireless communication systems have the ability of message authentication with no extra bandwidth consumption. Again, this technique studies message authentication while we focus on user authentication.

4) Physical Layer Challenge Response Authentication: Recently, a physical layer challenge response authentication mechanism, named PHY-CRAM, was proposed [11]. It utilizes the randomness of the fading channel to hide the shared secret used for authentication. PHY-CRAM does not require the legitimate user to be at a fixed location. It does not require a high-end signal analyzer or signature training. It is impossible for an attacker to pass the authentication by replaying the signal since a fresh nonce is used for every new authentication. It also favors dynamic environments.

PHY-CRAMR is an extension of PHY-CRAM to support authentication for two-hop wireless networks with a relay. It is secure when the relay is trustworthy. PHY-AUR uses a different methodology to tackle the problem of untrusted relay.

B. Conventional Challenge Response Authentication

Conventional challenge-response authentication mechanisms (such as CRAM-MD5 [18], CHAP [19]) use hash function to hide shared secret for authentication. The authentication mechanisms proposed in this paper is fundamentally different from the conventional ones. The fundamental difference lies in that PHY-CRAMR and PHY-AUR utilize physical layer properties to mask the shared secret used for authentication while conventional challenge-response protocols rely on cryptographic functions to hide the shared secret. The security strength of PHY-CRAMR and PHY-AUR depend on the randomness of the fading channel and the relative geographic location among the attacker, relay and legitimate users, but not depend on the computation complexity. As a result, both mechanisms do not suffer the threat of ever-increasing computing power, while this does not hold for conventional authentication schemes (such as CRAM-MD5 [18] and CHAP [19]). It is anticipated that cryptography-based authentication requires longer keys in the future, while longer keys usually imply higher computation overhead, communication overhead, energy consumption, and storage overhead.

Neither PHY-CRAMR nor PHY-AUR intends to replace the existing conventional challenge-response authentication protocol, but they can serve as attractive alternatives that do not depend on computational security.

III. System Model

A. Application Model

Real-world wireless communications usually involve two hops, such as two WLAN clients communicate with each other via an access point, or two mobile phones talk to each other through a base station. This paper provides new challenge-response authentication solutions at the physical layer for two-hop wireless networks.

The general application model is shown in figure 1. We consider two legitimate users Alice ($A$) and Bob ($B$), who communicate with each other with the assistance of Relay ($R$). An attacker may listen to the wireless channel, try to steal some useful information and impersonate a legitimate user.

In this paper, we mainly focus on one-way authentication in which $A$ needs to authenticate $B$. We assume $A$ and $B$ share a secret key $K$. The security of the authentication mechanisms rely on the shared secret key and the unique characteristics of the wireless fading channel.

B. Physical Layer Communication

At physical layer, we assume Orthogonal Frequency Division Multiplexing (OFDM) is adopted. OFDM is widely used in
current WLAN and cellular networks, such as WiFi 802.11a/n, LTE (4G), etc.

In OFDM systems, the bandwidth is shared by $N$ independent narrow band sub-carriers which can be multiplexed easily by Fast Fourier Transform (FFT) or Inverse Fast Fourier Transform (IFFT) operations. Due to this feature, it is convenient to conduct reciprocal and multiplication operations in the frequency domain. If not specified, all wireless signals and their operations are expressed in frequency domain in this paper.

Some sub-carriers in OFDM symbols are usually used as pilots for channel estimation. However, we eliminate pilots to avoid revealing the channel state information to the attacker. In fact, in the two protocols proposed, all OFDM symbols do not include pilots, synchronization preambles or any other reference signals, so that any receivers cannot estimate the channel and cannot get the original message further. In this case, autocorrelation on energy and cyclic prefix (CP) [20] is used for time synchronization at the receiving side.

In order to be close to the practical situation, both Rayleigh fading channel and Additive White Gaussian Noise (AWGN) channel are taken into account in the simulations.

C. Attack Model

The attackers can be either passive or active. A passive attacker can overhear all the signals transmitted from $A$, $B$, or $R$, and attempts to determine the authentication key. An active attacker not only can eavesdrop all the signals from $A$, $B$, or $R$, but also can inject or replay signals into the network.

The attacker can be inside or outside of the communication system. Relay node $R$ can be an inside attacker, who can record all the signals received from $A$ or $B$, and replay the signals later on or inject any signals into the network. $R$ may attempt to determine the authentication key or pass the authentication procedure by injecting specific signals without being noticed.

We do not consider jamming or denial of service attack (DoS) in this paper. All wireless communications are subject to this kind of attack, and counter jamming methodologies, such as frequency hopping [21], [22], can be incorporated into the physical layer authentication mechanisms proposed in this paper.

IV. PHY-CRAMR PROTOCOL

In this section, we propose PHY-CRAMR to provide physical layer authentication in wireless networks with relay. PHY-CRAMR actually is the extension of the existing PHY-CRAME protocol [11].

A. Basics

From the physical communication model described in section III-B, we denote $H_{AB}$ as the frequency domain channel response of fading channel and $W_{AB}$ as the AWGN for the wireless link from $A$ to $B$. $H_{AB}$ is the multiplicative factor to the frequency domain signal, while $W_{AB}$ is additive. Due to the use of IFFT/FFT in OFDM, we can always operate the signal in frequency domain conveniently. Equation (1) expresses the relationship between the received signal and transmitted signal.

$$RX_{AB} = TX_{AB}H_{AB} + W_{AB}$$  (1)

where $RX_{AB}$ and $TX_{AB}$ represent received and transmitted signals in the frequency domain respectively. $H_{AB}$ is a random process and provides a natural mask for the protocol messages.

In the design, we assume the channels are symmetric which means $H_{AB} = H_{BA}$ and keep correlated during the processing time. This is feasible because the processing time can be much smaller than channel coherent time $T_C$ in the real world. For example, we can adopt 2.4 GHz RF carrier, same as Wi-Fi frequency band. When transmitter and receiver have low relative speed $1m/s$, the Doppler frequency $f_d = v/\lambda = v f/c = 1 \times 2.4 \times 10^6/(3 \times 10^8) = 8Hz$. Empirically, coherent time is related to maximum Doppler frequency shift and can be calculated as $T_C = \frac{9}{16 \pi f_d} = \frac{9}{16 \pi \times 8} = 0.02239s = 22.4ms$. In the mobile environment with relative speed $v = 60km/h$, the corresponding coherent time is $1.3ms$ calculated in the same way. On the other hand, the total process time may include transmitting time $T_t$, propagation time $T_p$ and operation delay $T_d$ in each nodes. If we take $10MHz$ sampling rate, an OFDM symbol with 64 sub-carriers and 16 CP samples takes $T_t = 8\mu s$ to transmit. The propagation delay will be $1\mu s$ if the distance is $300m$. The operation delay is usually in the same order of transmitting time. Then totally the processing time can be much smaller than coherent time in the above two cases.

B. Protocol Description

PHY-CRAMR is a challenge-response protocol with only one round procedure, as illustrated in figure 2. For easy understanding and description purpose, we ignore AWGN and assume channel reciprocity holds in the illustration. Noise and non-perfect channel reciprocity will be taken into account in the later analysis.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{PHY-CRAMR.png}
\caption{PHY-CRAMR protocol}
\end{figure}

\textbf{Step (0)} At time $t_0$, $B$ sends one OFDM frame with the authentication request. Only one symbol is needed to identify the request command. This starts the protocol.

\textbf{Step (1-1')} After receiving the authentication request from $B$, $A$ randomly generates a random number $n$ (i.e., challenge) to modulate amplitudes of sub-carriers in one OFDM symbol, and sends it to $R$. What $R$ receives is $nH_{AR,t_1} + W_{AR}$, where $H_{AR,t_1}$ is the wireless channel at time $t_1$ between $A$ and $R$ and $W_{AR}$ is the AWGN. $R$ further forwards the received signal to $B$.

\textbf{Step (2-2')} After $B$ receives the signal from $R$, it calculates the reciprocal (inverse) of the received signal, multiplies it by the shared key $K$, and then transmits the resulting signal to $R$. In the same way, $R$ forwards the signal to $A$.

C. Verifying Scheme

After the frame is arrived, $A$ verifies the authentication message from $B$. If AWGN is ignored, the signal received by $A$ can be expressed as the first half part in equation (2).

$$RX_{A,t_2} = \frac{T}{nH_{AR,t_1}H_{RB,t_1}}H_{BR,t_2}H_{RA,t_2} \approx \frac{K}{n}$$  (2)

If the processing time is smaller than the channel coherent time $T_C$, which can be ensured in practice, the channel effects can be
Further cancelled out due to the symmetric correlated channel. That is \( H_{AR,t_2} = H_{RA,t_2} \) and \( H_{RB,t_2} = H_{BR,t_2} \). Then, after the last step, \( A \) can calculate the approximate shared key \( K' = nRX_{A,t_2} \approx K \). Finally, \( A \) can verify the message by comparing \( K' \) and \( K \). However, because of non-perfect channel reciprocity and especially AWGN, the estimated \( K' \) will be different from the real one, but should be highly correlated. Therefore, we use the method of correlation to evaluate the similarity between \( K \) and \( K' \). Then verifier can make the judgement whether it is talking to \( B \) according to the predefined threshold and the correlation result between calculated \( K' \) and \( K \). The correlation of two variables \( i \) and \( j \) is defined in equation (3).

\[
Corr(i, j) = \frac{Cov(i, j)}{\sqrt{Cov(i, i)Cov(j, j)}}
\]

(3)

Here, \( Cov \) is the covariance of two variables.

\[
Cov(x_1, x_2) = E[(x_1 - \mu_1)(x_2 - \mu_2)]
\]

(4)

where \( E \) is the mathematical expectation, \( \mu_1 = E(x_1) \) and \( \mu_2 = E(x_2) \).

The absolute value of correlation result ranges from 0 to 1. As we know, the higher the correlation is, the more similar the two values are. A parameter, \( 0 < C_0 < 1 \), can be set as the threshold. If the equation (5) is satisfied, \( A \) believes the counterpart \( B \) is really what it claims. Then \( B \) passes the authentication.

\[
Corr(nRX_{A,t_2}, K) > C_0
\]

(5)

The selection of threshold \( C_0 \) is critical. A large \( C_0 \) may lead to a high false negative rate, which means many legal users may not pass the authentication. On the other hand, a small \( C_0 \) may lead to a high false positive rate, which means many illegal users may pass the authentication. Therefore, we should make a trade-off to balance them. The Receiver Operating Characteristic (ROC) curve, which reflects the relationship between successful authentication rate (the rate of legitimate users who pass the authentication) and false acceptance rate (the rate of illegal users who pass the authentication), will be used to evaluate the protocol’s performance.

For the ideal case, when AWGN is ignored and channel symmetrical characteristic is considered, that is \( H_{XY} = H_{YX} \), we can easily get \( Corr(nRX_{A,ideal}, K) = Corr(K, K) = 1 \). Therefore the verification scheme is correct. Actually, the performance will be worsened mainly by AWGN, because we can consider the channel is symmetric between two nodes as long as the processing time is smaller than \( T_{C} \) which can be ensured in practice. The performance with different SNR will be shown in our simulation in section VI-E to examine the effects of AWGN.

**D. Data Mapping**

Figure 3 shows the general OFDM system. The original bit stream is mapped to sub-carriers in OFDM symbols before IFFT operation for multiplex. In this subsection, we will mainly discuss the data format used and the data mapping.

In the one round challenge-response message exchanges described above, the shared key and random challenge number are the authentication messages. The length of \( K \) and \( n \) can be different, but it will be convenient to use the same bit length \( L \). Then \( K = \{K_0, K_1, ..., K^{L-1}\} \) and \( n = \{n^0, n^1, ..., n^{L-1}\} \), where \( K^l \in \{0, 1\} \) and \( n^l \in \{0, 1\} \) for \( l \in \{0, 1, ..., L - 1\} \).

In practice, there are mainly three kinds of sub-carriers in an OFDM symbol: data sub-carriers used to transmit data, pilot sub-carriers used for channel estimation, and null sub-carriers to protect side band and DC sub-carrier. For different modulation mapping scheme, different number of bits from original messages are mapped to each data sub-carrier sequentially in OFDM symbols. Usually, a complex value, in which the real part and imaginary part represent In-phase and Quadrature component respectively, is used as the mapped signal for each sub-carrier in OFDM systems. For example, in QPSK mapping, a frequently-used method, two bits are mapped to a complex number for each sub-carrier, and then there are totally four states.

In this paper, we adopt AM as the mapping scheme. We assume there are \( S \) bits per sub-carrier. Then the number of total data sub-carriers used for \( K \) or \( n \) is \( M = \lceil L/S \rceil \), where \( \lceil \cdot \rceil \) denotes the operation that rounds a number toward positive infinity. Then \( \lceil M/N \rceil \) symbols in one transmitting frame are needed to accommodate all the information in \( K \) or \( n \). If there are \( N \) data sub-carriers in each OFDM symbol. For simplicity, we choose \( M < N \) so that only one symbol can carry all bits in \( K \) or \( n \). In this following description, we take the sub-carrier number \( M \) as the key length. A brief mapping relationship for the case of \( M < N \) is shown in figure 4.

![Fig. 3. General OFDM system](image)

![Fig. 4. Data mapping in OFDM symbol (M < N, SC represents sub-carrier)](image)

In fact, both the length of the shared key \( M \) and the bit number for a sub-carrier \( SC \) will affect the correlation results in the verifying scheme and further influence the overall performance. Different \( M \) will be examined in our simulations for comparison.

We can define an AM mapping rule which can reflect the relationship between S-bit data and the mapped complex number. However, as a simplification, we can generate \( M = \lceil L/S \rceil \) complex numbers with random absolute values and random phases to represent original message \( K \) and \( n \) directly.

Since we only exploit the amplitude components in AM, the phase components are ignored. The amplitude component is the real absolute value of the complex number in each sub-carrier, which ranges from \( A_1 \) to \( A_2 \). Because we do the reciprocal in PHY-CRAMR, \( A_1 \) and \( A_2 \) cannot be too large or too small so as to avoid signal peaks and high transmission power at some sub-carriers. Meanwhile, \( A_2/A_1 \) should be large enough to keep a good discrimination and hide the channel state information. In fact, the distribution range of the amplitudes in sub-carriers should be in accordance with channel’s magnitude response.
E. Security Analysis

The use of random challenge number $n$ in step (1-1') can ensure different messages for each authentication and prevent simple replay attack. Due to the missing of pilots, synchronization preambles and any pre-known reference signals in transmitting signals, an attacker cannot estimate the channel information to extract the authentic message. Legitimate users $A$ and $B$ in the system share one secret key. All of these ensure the security of the protocol. For any attacker $E$, we denote the wireless channel between $E$ and $A$, $B$ and $R$ as $H_{AE}$, $H_{BE}$ and $H_{RE}$, respectively.

1) Passive Attacks: A passive attacker $E_P$ only monitors the network traffic and try to obtain useful information such as shared key $K$, for the further attack. Passive attacker will not inject additional signals during the authentication process. Different locations will result in different abilities for attacks.

(1) The naive $E_P$: When passive attacker $E_P$ is far away from $A$, $B$ and $R$, the exchanged messages between $A$ and $B$ are masked by the channel naturally. We name this kind of passive attackers as naive $E_P$, because it can obtain little information about the authentic message. In PHY-CRAMR, $E_P$ can intercept four messages ($nH_{AE}$, $nH_{AR}H_{RE}$, $KH_{BE}/(nH_{AR}H_{RB})$, $KH_{RE}/(nH_{AR})$) if AWGN is ignored and symmetric channel is assumed, where seven unknown factors ($K$, $n$, $H_{AE}$, $H_{BE}$, $H_{RE}$, $H_{AR}$ and $H_{BR}$) exist. $E_P$ cannot determine $K$ through these messages because it has no knowledge about any channel state information.

(2) The smart $E_P$: Similar to [11], a smart $E_P$, who is very close to one certain legitimate user, may get more information. If $E_P$ is very close to $A$, $H_{AE}$ is close to 1 because the line-of-sight (LOS) signal is much stronger than any other multipath signals and $H_{RE}$ is close to $H_{AR}$. Then the messages $E$ can receive are simplified as $(n, nH_{AR}^2, KH_{BE}/(nH_{AR}H_{RB}), K/n)$. In fact, $E$ who is close to $A$ can get approximate values of $n$ and $K$ in this situation. This is why the protocol security relies on location decorrelation and stochastic property of the wireless channel. If the channel is a pre-known constant, it should not be safe. When $E_P$ is close to $B$, $H_{BE}$ is close to 1 and $H_{RE}$ is close to $H_{BR}$. When $E_P$ is close to $R$, $H_{RE}$ is close to 1. Similar to the case that $E_P$ is close to $A$, the attacker can derive the approximate value of $K$ in both of these two cases. However, this kind of attack is hard to launch, because as we know, more than half a wavelength ($\lambda/2$) distance is essential to keep the wireless channel uncorrelated. If 2.4 GHz frequency is used, then $\lambda/2 = 6.25$ cm, a very short distance within which an attacker can be easily identified by the legitimate users. Then $E_P$ can only derive a roughly estimated $K$ due to location distinction, while legitimate users have perfect knowledge about $K$ [11].

(3) Untrusted relay $R$: There is a special case that the relay $R$ is an adversary. Because all the message for authentication are relayed by $R$, it can have more information. Actually, $R$ can easily get the shared $K$, because it knows $nH_{AR,t_1}$ after step 1 and $KH_{BE}/(nH_{AR}H_{RB})$ after step 2. Then $R$ can obtain $K$ by multiplying two received signals. In this case, $R$ can forge the protocol signal in step 2' next time. Thus, although the idea may be suitable for one hop, it is not secure for multi-hop cases if the relay is not trustworthy.

2) Active Attacks: The active attacker $A$ can inject or replay signals based on what it obtained. As we assumed, we do not talk about the jamming and DoS attacks.

In a replay attack, $E_A$ wants to pass the authentication using the information it intercepts during the process of legal authentication in previous rounds. However, $E_A$ cannot succeed because the challenge $n$ sent from verifier $A$ is randomly selected at each time. The old one cannot be used for the new authentication.

Due to the pilots elimination method, outside users cannot estimate the wireless channel and extract the original message. Then it is also very hard for outside attacker to mimic the authentication messages.

However, an untrusted relay $R$ is a threat to this protocol. As we discussed before, attacker $R$ can derive shared key $K$. Then in the next time, it can forge a message in step 2' based on $K$ and what it received in step 1.

Further more, if the relay $R$ is not honest, outside users can also launch impersonation attack with the assistance of $R$. What outside attacker $E_P$ can receive after step 1 is $nH_{AR}H_{RE}$. Then it does the reciprocal operation and transmits the result to $R$. $R$ can receive $1/nH_{AR}$. Now that $R$ has the ability to determine $K$, it can construct the message $K/nH_{AR}$ for $E_P$. Finally, $E_P$ will pass the authentication. In fact, this kind of joint attacks can be detected if $A$ always sends the challenge $n$ after the legal authentication request. In this case, the legitimate prove $B$ also exists in the system. $B$ will also respond in the authentication process. Therefore, we can keep the received signal strength (RSS) at a certain level. If there are other responses, the RSS will be higher than normal level. Then we can avoid it by maintaining and detecting RSS.

F. Extension for More Hops

Actually, the protocol is not limited for two hops. Figure 5 shows the general case of PHY-CRAMR in multi-hop networks. In each hop, the channel effects will accumulate. Because of more additive noise involved, the performance will get worse with increased hop count. The simulation result for multiple hops is shown in figure 12.

V. PHY-AUR PROTOCOL

As discussed in the previous section, PHY-CRAMR works under the assumption of a trusted relay, but fails when the relay launches an inside attack. In this section, we propose a new protocol, PHY-AUR, to defend against the inside attack from an untrusted relay. In fact, the attack from the untrusted relay is hard to resist because all exchange signals can be recorded or relayed by $R$. Based on this, $A$ and $B$ should share more secret information which $R$ and other attackers cannot obtain.

A. Protocol Description

In this scheme, we keep the same basic assumptions as in PHY-CRAMR, such as the data mapping method and pilots elimination in OFDM symbols. The difference lies in that two shared key $K_1$ and $K_2$ are used and two OFDM symbols are transmitted simultaneously as one signal frame in each step. $B$ requests the authentication first and the protocol still needs only one round message exchange. The protocol is illustrated in figure 6 by ignoring noise.

Step (0) $B$ sends one OFDM frame with the authentication request.

Step (1-1') $A$ generates a random number $n$, and sends $K_1$ and $n$ in two consecutive OFDM symbols which will undergo the same channel fading because of short time interval with different AWGN. $R$ just forwards the received signal to $B$. At $B$’s side, it can calculate $n/K_1$ by dividing two received symbols and further get the estimated $n'$ easily with the known shared $K_1$. The same as PHY-CRAMR, AWGN will influence the performance seriously.
C. Security Analysis

1) Passive Attacks: A passive attacker $E_P$ only monitors the traffic from wireless channel in order to acquire some information about shared key $K$, and does not transmit signals during the authentication process.

   (1) The naive $E_P$: Messages what $E_P$ can receive are

   \[
   \begin{align*}
   &\{ K_1H_{AE}, K_1H_{AR}H_{RE}, K_2H_{BE}, K_2H_{BR}H_{RE} \\
   &nH_{AE}, nH_{AR}H_{RE}, nH_{BE}, nH_{BR}H_{RE} \}
   \end{align*}
   \]  
   (8)

   For naive attackers, $E_P$ still has no way to guess the shared key $K_1$ and $K_2$ from the received messages in PHY-AUR, because the original messages are masked by random channels and attackers cannot obtain the channel information, as discussed in IV-E. As a result, both PHY-CRAMR and PHY-AUR are safe under this kind of passive attacks. The correlation distributions in the verifying step of two protocols for legitimate users and attackers are compared in figure 11 in our simulation section.

   (2) The smart $E_P$: If $E_P$ is very close to $A$, we can assume $H_{AE} \approx 1$ because of the LOS signal and $H_{RE} \approx H_{AR}$. Then smart $E_P$ can obtain the following signals from equation (8).

   \[
   \begin{align*}
   &\{ K_1, K_1H^2_{AR}, K_2H_{BE}, K_2H_{BR}H_{AR} \\\n   &n, nH^2_{AR}, nH_{BE}, nH_{BR}H_{AR} \}
   \end{align*}
   \]  
   (9)

   In fact, the attacker can derive the approximate $K_1$, $K_2$, and $n$. When $E_P$ is very close to $B$, the situation is similar because the messages $A$ and $B$ transmitted are symmetric. When $E_P$ is very close to $R$, $H_{RE} \approx 1$, $H_{AE} \approx H_{AR}$ and $H_{BE} \approx H_{BR}$. Then equation set (8) can be simplified as $(K_1H_{AR}, nH_{AR}, K_2H_{BR}, nH_{BR})$ with five unknown values $(K_1, K_2, n, H_{AR}, H_{BR})$. Therefore, $E_P$ cannot solve the equation set. The smart attack is hard to launch since distinct locations make wireless channels uncorrelated.

   (3) Untrusted relay $R$: Untrusted relay is a special case when the smart attacker $E_P$ is right at the position of $R$, that is, $H_{RE} = 1$, $H_{AE} = H_{AR}$ and $H_{BE} = H_{BR}$. From discussions above, the untrusted relay cannot obtain shared key $K_1$ and $K_2$. Even when we use one same shared key $K_1 = K_2 = K$, $R$ can only compute $K_1/n = K_2/n = K/n$ and $H_{AR}/H_{BR}$ at most, without individual information about $K_1$, $K_2$, $n$, $H_{AR}$, and $H_{BR}$. That is PHY-AUR can prevent the passive attacks even if the relay is not honest, which is different from PHY-CRAMR.

2) Active Attacks: Different from passive attacks, an active attacker $E_A$ may pretend to be an legitimate user even it has no knowledge about the shared key.

   In our initial design, we use one shared key $K = K_1 = K_2$ instead of two individual keys. In that case, passive attacks can be avoided from the discussion above. However, the untrusted relay $R$ and other outside attackers may impersonate the legitimate user. As we know, $R$ can receive $RX_{R_1} = (KH_{AR}, nH_{AR})$ after step 1 and $RX_{R_2} = (KH_{BR}, nH_{BR})$ after step 2. Then $RX_{R_2} = RX_{R_1}X$ is what $R$ forwards in step 2’, where $X$ is a coefficient. In fact, the untrusted $R$ can multiply the received signal $RX_{R_1}$ by any coefficient and send the result to $A$ in step 2’, because any coefficient can be cancelled out after $A$ does the division operation. Finally, $A$ can still extract correct $n$ and pass the authentication. Furthermore, for an outside attack $E_A$, he can receive $RX_{E_A} = (KH_{AR}H_{RE}, nH_{AR}H_{RE})$. In the same way, he can impersonate legitimate user $B$ and forge a message by multiplying $RX_{E_A}$ and any coefficient. Then $A$ can also derive the right challenge $n$ even with a trusted relay. Base on this observation, two individual shared keys are used to prevent the impersonation and replay attack, because $RX_{R_1}$ and $RX_{R_2}$ keep the multiplicative relationship no longer. The prover needs to calculate the challenge $n$ first and then send back $(K_2, n)$. Any other users cannot forge the message in step 2’ and cannot succeed in the authentication.

   Actually, PHY-AUR defends against an active attacker $E_A$ through three features: (1) two different shared key are used; (2)
all signals defined in the protocol do not have pilots or pre-known preambles for channel estimation; (3) legitimate users maintain the received signal strength (RSS) of all signals except for the authentication request, within the expected range. Feature (3) is feasible because path-loss in both directions at all links are identical during channel coherence time, and the path-loss from prover to relay and from relay to verifier are measured during the transmission of request which has constant power.

If $E_A$ pretends to be the verifier $A$, it must wait until a legitimate prover initiates a conversation with it coincidentally. However, since the real verifier also exists in the network, both the verifier and $E_A$ will respond to the prover, the RSS at relay exceeds the expected range, and the relay can easily detect $E_A$. Similarly, the prover can detect $E_A$ who pretends to be the relay.

3) Others: The challenge and response messages do not necessarily travel the reversal path, since $A$ and $B$ can decode the messages using the share key. This is different from PHY-CRAMR. However, the interval between the challenge and response messages should be short to avoid unnecessary security issues. After all steps are finished, $n$ and $H_{AR} H_{RB}$ are shared by two participants and can also be used to generate session key $SK = F(n, H_{AR} H_{RB})$ for the further secure communications. We do not intend to discuss key generation function $F$ in depth here, which is out of the scope of our considerations. The protocol can implement authentication and key generation simultaneously with two shared keys $K_1$ and $K_2$ between $A$ and $B$ in multi-hop wireless networks. Even if the authentication is false accepted, the shared session key $SK$ originated from $n$ and $H_{AR} H_{RB}$ cannot be obtained by the adversary.

D. Extension for More Hops

PHY-AUR is also scalable and can be extended to networks with more hops. The general case of PHY-AUR in multi-hop networks is shown in Figure 5. Similar to PHY-CRAMR, the channel effects will accumulate in each link. The simulation result for multiple hops is shown in figure 12.

PHY-AUR utilizes the dividing operations to cancel out the channel effects, while PHY-CRAMR makes it by the reciprocal of the channel effects will accumulate in each link. The simulation result for multi-paths is shown in figure 12.

VI. Performance Evaluation

The random wireless fading channel and AWGN will affect the performance of the protocols. PHY-CRAMR requires short processing time to limit the time-varying nature of the channel, while PHY-AUR is not sensitive to it. Both the fading and AWGN can worsen the signal quality, and the stochastic property and location decorrelation of the channel make the attacks difficult. The performance of the proposed protocols is evaluated by the ROC, which reflects the relationship between successful authentication rate and false acceptance rate. The steeper (higher) the ROC curve is, the better the performance.

A. Simulation Settings

We conduct our simulations in MATLAB. The sample rate is fixed to be 10 MHz. Each OFDM symbol includes $N = 64$ data sub-carriers and Guard Interval has $GI = 16$ samples. The shared key $K$ and the random challenge $n$ are both complex vectors with the same length $M (\leq N)$. They are put into OFDM symbols sequentially. The ROC curve comes from 1000 iterations which represent 1000 pairs of authentication procedures. SNR ranges from 10 dB to 30 dB. The statistical Rayleigh fading channel model is adopted and can be configured conveniently in MATLAB. The rural and urban channels are differentiated by $MP = 10$ and $MP = 20$ multi-paths, respectively. The delays for multi-paths are randomly selected and the corresponding gains are normalized. The maximum delay spread is $\Delta = \frac{16MSa}{15MSa/\mu s} = 1.6\mu s$, the same time span of GI. Figure 8 shows an example of frequency response of the channel with 20 multi-paths.

B. Impact of Channel

When key length $M = 60$, at different SNR, the ROC curves for PHY-CRAMR in rural and urban channel models are shown in figure 9(a) and 9(b), while PHY-AUR are shown in figure 9(c) and 9(d). The performance in the rural environment is better than in the urban area, because of fewer multi-paths which impact signal quality. Higher SNR results in better performance for both channel models. As we expected, more AWGN leads
to worse performance. As the figures illustrate, the successful authentication rates almost reach 100% for both protocols under both channel models when $M=60$ and SNR $> 10$ dB.

C. Impact of Key Length

The length $M$ of $K$ and $n$ is also a parameter that affects the performance. In figure 10(a) and 10(b), we can see that the impact of key length on the performance of PHY-CRAMR is not significant when SNR=20 dB. Under this condition, a key length of 40 already achieves almost 100% successful rate. However, figure 10(c) and 10(d) show that the performance of PHY-AUR improves with increased key lengths. This may be due to the operation of correlation when verifying authentication. The longer length results in a more accurate estimation of the correlation.

![Fig. 7. General case of PHY-AUR in multi-hop networks](image)

![Fig. 10. ROC curves with different key length $M$ when SNR=20 dB](image)

![Fig. 11. CDF of correlation distributions under different SNRs (MP=10, M=60)](image)

D. Correlation Distribution

We can also take a look at the distribution of correlations calculated in the verifying steps further. Figure 11 shows the cumulative distribution function (CDF) curves of correlation distributions in two protocols with multipath number $MP=10$, key length $M=60$ and different SNRs. When SNR increases, both protocols can gain relative higher correlations for legitimate users. The attackers, who can only guess the shared key shared, keeps a constant correlation distribution under different SNR, and the value is much lower than the results from legitimate users.

E. Impact of Relay Number

Both PHY-CRAMR and PHY-AUR have the potential to be extended to wireless networks with more hops. We also conduct simulations with more relays in the wireless networks. Figure 12 shows the simulation result for different number of relays when SNR=20 dB. When the hop count increases, the performances of both mechanisms degrade due to signal path loss and accumulated noise. Signal amplification and noise mitigation mechanisms can be integrated to improve the performance.

VII. Discussion

A. Two-way Authentication

Secure communications usually require the participants to authenticate each other. Although only the one-way authentication mechanism is discussed, the two-way authentication can be implemented in the same way. The communication overhead can be doubled.
B. MIMO Enhancement

MIMO technology can be used to further improve the security strength since longer authentication keys can be conveyed using the same amount of time. Beamforming mechanism can be applied to achieve energy efficiency and tackle channel diversity.

C. Heterogeneous Network

Both PHY-CRAMR and PHY-AUR can be applied to heterogeneous networks or cognitive radio networks while different hops may use different channels or frequencies. The transmission rate at different hops may need to change in order to adapt to different channel conditions and bandwidths.

VIII. CONCLUSIONS

We proposed two authentication protocols based on challenge-response mechanism, named PHY-CRAMR and PHY-AUR, at the physical layer for wireless networks with a relay. OFDM technique is adopted to modulate the challenge and response messages. They both exploit the unique properties of wireless fading channel, such as randomness and location decorrelation, to hide the authentic message. By eliminating pilots, pre-known synchronous headers, and any reference signals, the attacker cannot gain any knowledge about the channel state information and the secret messages between legitimate users. PHY-CRAMR provides a secure authentication solution when the trusted relay is assumed, while PHY-AUR is immune to both outside and inside attacks with an untrusted relay.

Both protocols are analyzed and simulated to verify the performance. The simulation results show that both PHY-CRAMR and PHY-AUR can obtain a high successful authentication rate and a low false acceptance rate under various channel environments.

Comparing with previous work, our schemes are simple, secure, robust and scalable in multi-hop wireless networks. Although unilaterally the procedures of the protocols are performed, the mutual authentication can be implemented further.

REFERENCES


